Mining Partially-Ordered Episode Rules in an Event Sequence

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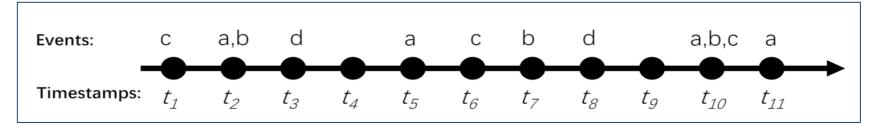






Frequent Episode Mining

Input: a sequence of events with timestamps



Output:

All frequent episode $(occurrence\ count \ge minSup)$

Episode Types:

- parallel episodes,
- serial episodes,
- complex episodes...

Algorithms:

WINEPI, MINEPI, EMMA, MINEPI+,

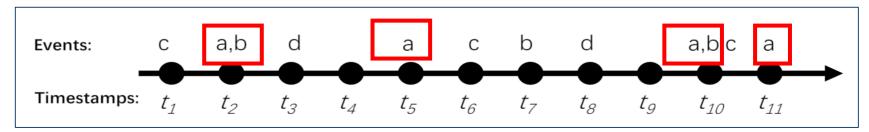
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Frequent Episode Mining

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Example:

episode <{a,b},{a}>

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Episode Rule Mining

Input: a sequence of events with timestamps

Events: c a,b d a c b d a,b,c a

Timestamps:
$$t_1$$
 t_2 t_3 t_4 t_5 t_6 t_7 t_8 t_9 t_{10} t_{11}

Output:

Each episode rule : $X \rightarrow Y$ such that:

$$(Supp(X) \ge minSup)$$

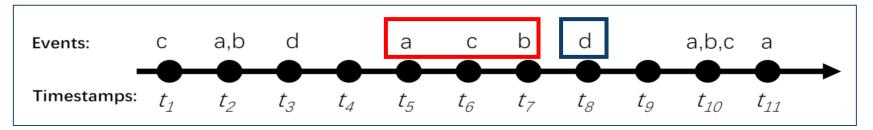
$$(conf(X \rightarrow Y) = \frac{Supp(X \cap Y)}{Supp(X)} \ge confidence)$$





Episode Rule Mining

Input: a sequence of events with timestamps



Output:

Each episode rule : $X \rightarrow Y$ such that:

$$\langle \{a\},\{c\},\{b\} \rangle \rightarrow \langle \{d\} \rangle$$

$$(Supp(X) \ge minSup)$$

$$(conf(X \rightarrow Y) = \frac{Supp(X \cap Y)}{Supp(X)} \ge confidence)$$





Related Work

- Frequent episode rules (1995, and many papers after)
- Utility-based episode rules (ASOC 2017)
 - Discovering episodes rule having a high importance in a sequence of discrete events with weights and quantities
- Precise-positioning episode rules (TKDE 2018, ICDE 2017)
 - the elapsed time between the antecedent and the consequent is fixed
- Distant and essential episode rules (ESWA 2018)
 - the antecedent is as small as possible in terms of number of events and of occurrence duration
 - consequent is temporally distant from the antecedent





An Important Limitation

Events within an episode rule must follow a <u>very strict</u> temporal ordering

Example:

$$\langle \{a\}, \{c\}, \{b\} \rangle \rightarrow \langle \{d\} \rangle$$

$$\langle \{a\}, \{b\}, \{c\} \rangle \rightarrow \langle \{d\} \rangle$$

$$\langle \{b\}, \{a\}, \{c\} \rangle \rightarrow \langle \{d\} \rangle$$

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But for applications such as analyzing transactions in a retail store, all these rules may be the same:

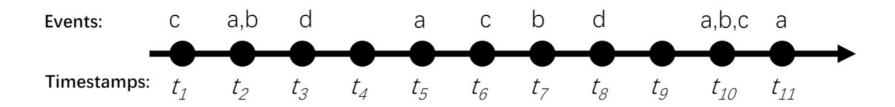
$$\{a, b, c\} \rightarrow \{d\}$$





Event set

An **event set** is a set of events. e.g. {a,b,c}

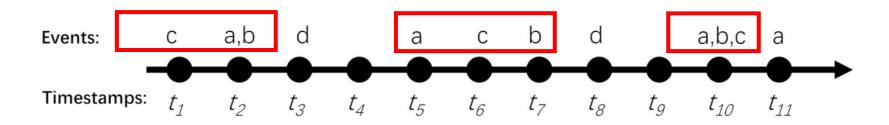






Event set

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The **non-redundant occurrences** of **{a,b,c}** are:

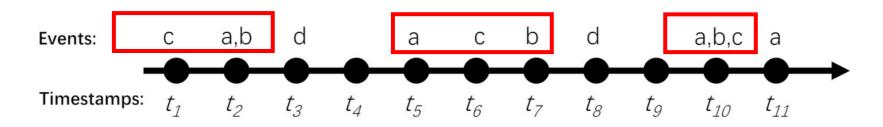
$$Occ({a, b, c}) = {[t_1, t_2], [t_5, t_7], [t_{10}, t_{10}]}$$





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$$Occ({a, b, c}) = {[t_1, t_2], [t_5, t_7], [t_{10}, t_{10}]}$$

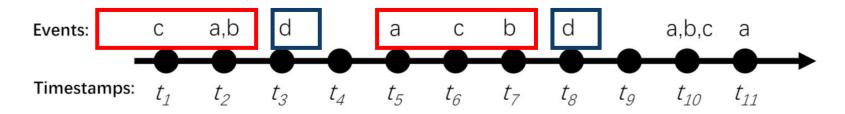
Note that a time interval such as $[t_{10}, t_{11}]$ is **redundant** to $Occ(\{a, b, c\})$ because $[t_{10}, t_{11}]$ is overlapping with $[t_{10}, t_{10}]$.





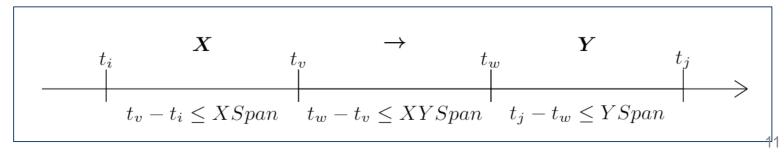
Partially-Ordered Episode Rule (POER)

A new type of episode rules that loosen the ordering constraint.



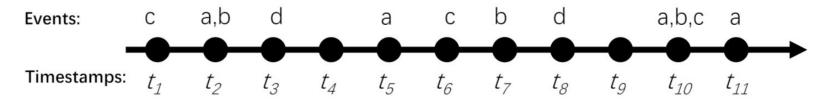
Example: $\{a, b, c\} \rightarrow \{d\}$ where occ(R) = {[t1, t3],[t5, t8]}

minsup= 3, minconf= 0.6, XSpan= 3, XYSpan= 1, YSpan= 1

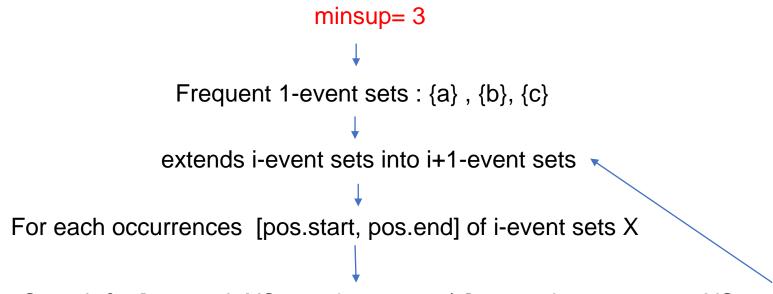




3. The POERM algorithm



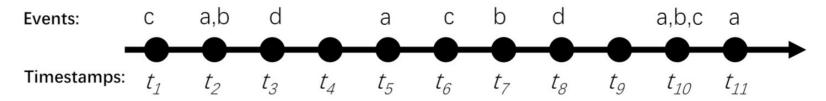
STEP 1: Find the frequent rule antecedents



Search for [pos.end-XSpan+1, pos.start),[pos.end+1, pos.start+XSpan), and [pos.start, pos.end] to extend it



3. The POERM algorithm



STEP 2: Find consequents to make rules

Frequent event sets : <{a} , {b}, {c},{a, b}, {a, c}, {b, c}, {a, b, c}>

Frequent 1-event consequent rule

Extends i-event consequent rule into i+1-event consequent



3 A Baseline Algorithm called POERM-ALL

Find all possible antecedents



Find all possible consequents



Concatenate antecedents with consequents to get POER candidates



Filter to obtain the POER rules



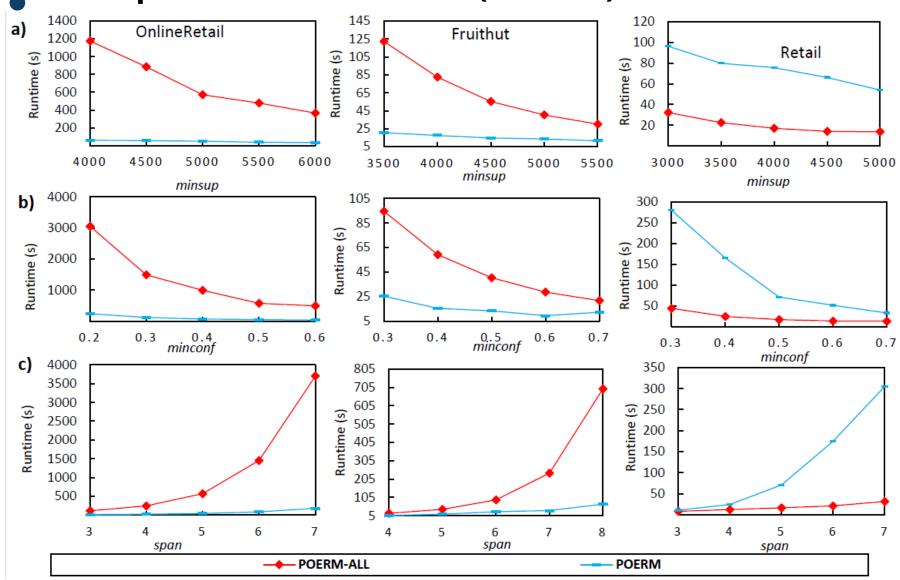
4 Experimental Evaluation

Dataset	# Timestamps	# Events	Average event set size
OnlineRetail	541,909	2,603	4.37
Fruithut	181,970	1,265	3.58
retail	88,162	16,470	10,30

Default Values	minsup	minconf	Span
OnlineRetail	5000	0.5	5
Fruithut	5000	0.5	5
retail	4000	0.5	5

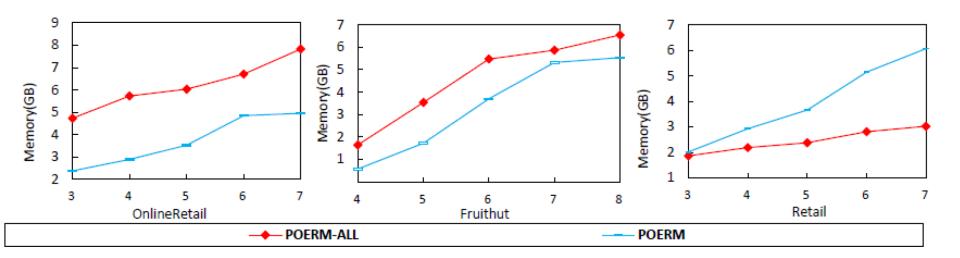


4. Experimental Evaluation (runtime)





4. Experimental Evaluation (memory)



- On OnlineRetail and FruitHut, POERM consumes less runtime and memory then POERM-ALL.
- But on sparse datasets such as Retail, POERM can't perform better than POERM-ALL.



4. Experimental Evaluation (patterns in real data)

These patterns were discovered in the Fruithut dataset:

L		
Rule	$\operatorname{occ}(X \to$	Y) occ(X)
Cucumber Lebanese, Field Tomatoes→Banana Cavendish	4910	6152
Capsicum red, Field Tomatoes→Banana Cavendish	5033	6352
Broccoli, Capsicum red→Field Tomatoes	2343	4043
Nectarine White→Watermelon seedless	2498	5687
Garlic loose, Field Tomatoes→Capsicum red	1752	4409
Cucumber Lebanese, Capsicum red $\rightarrow \!$	1236	4098



Contributions:

- >A novel type of rules called partially-ordered episode rules
- ➤ An efficient algorithm named POERM (Partially-Ordered Episode Rule Miner) to find these rules
- ➤ Experimental evaluation on several benchmark dataset shows that POERM has excellent performance and find interesting rules.

•Future work:

- >POERM for streaming data and big data.
- ➤ Considering more complex data types

≻Open-source code, datasets:

> SPMF data mining library (over 200 algorithms)

Thanks for listening!

The timestamps that are searched for a candidate ruleX→Y

